

MANY QUESTIONS AND FEW ANSWERS ON EXPONENTIAL BASES

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An exponential basis on a domain $D \in \mathbb{R}^d$ is a Riesz basis of $L^2(D)$ made of exponential functions with linear exponents. Exponential bases are very useful in the applications but they are difficult to come by. Only a few domains of \mathbb{R}^d are known to have exponential bases, and there is no example of a domain on which exponential bases are known not to exist. In this talk I will present a number of problems on exponential bases. In particular, I will discuss the following problem: let D be a domain of measure 1 and let B be an orthonormal exponential basis on the unit cube of \mathbb{R}^d . Can B be a frame, or a Riesz basis, or a Riesz sequence on D ?

Joint work with Alberto Mizrahi (Florida International University) and Alex Tepper (Florida International University).