Fractional elliptic problems with nonlinear gradient sources and measures

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In this talk, we will deal with the study of existence and regularity of appropriate weak solutions for non-local quasi-linear problems involving measures:

(1)
$$\begin{cases} (-\Delta)^{\alpha} u(x) &= g(x, |\nabla u|) + \sigma \nu \quad \text{in } \Omega, \\ u(x) &= \varrho \mu \quad \text{in } \mathbb{R}^N \setminus \Omega, \end{cases}$$

where $\rho, \sigma \geq 0$, μ and ν are suitable Radon measures, $g: \Omega \times [0, \infty) \to [0, \infty)$ is a continuous function fulfilling certain growth conditions (to be presented *a posteriori*) and $\Omega \subset \mathbb{R}^N$ is a C^2 bounded domain. We shall discuss different regimes where a solution may be defined and we will extend the presentation to Dirichlet problems like (1) with the addition of measures concentrated on the boundary $\partial\Omega$.

This is a joint work with Analia Silva from Universidad Nacional de San Luisconicet and Joao Vitor da Silva from Universidad de Brasilia.